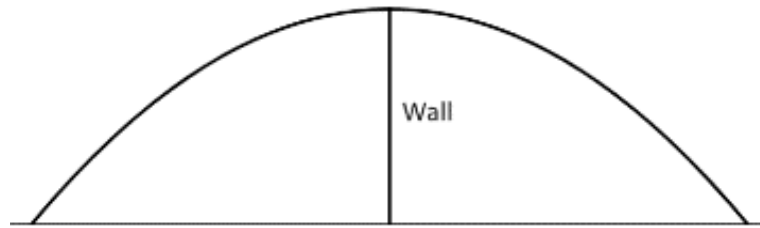


Projectiles – www.m4ths.com – Steve Blades ©

(1) A particle is projected from the ground with velocity $U\text{ms}^{-1}$ at an angle of θ . The particle travels $X\text{m}$ in T seconds before hitting the ground. The particle just clears a wall of height $Y\text{m}$ as shown below



(a) Given that the distance of the wall from the point of projection is $0.5X$, show that $T = \frac{2U}{g} \sin \theta$

(b) Given further that $\tan \theta = 0.75$, show that $Y < \frac{9U^2}{50g}$

(2) A particle is projected at point O with velocity $(6i + 12j)\text{ms}^{-1}$ towards a moveable ledge.

(a) Given that the ledge is initially 8m above O , show that the particle cannot land on the ledge.

(b) The ledge is now lowered to a point 5m above O . The particle is launched and lands on the ledge. Find the maximum horizontal distance of the ledge from O .

(c) Find speed the particle hits the ledge with at the distance found in part (b).

(3) A particle is launched from a point 40m above the ground with velocity $(20i - 3j)\text{ms}^{-1}$. Find the angle the velocity of the projectile makes with the ground as it strikes the ground.

(4) A particle is projected from a point A with velocity 16ms^{-1} at angle of 50° to the horizontal. Find the horizontal distance travelled when the particle is more than 2m above A .

(5) A particle is projected from a point 30m above the ground with velocity 20ms^{-1} at an angle α . The particle hits the ground after 2 seconds.

(a) Show that $-30 < \alpha < 0$

(b) Given instead the particle is projected at an angle θ , find the maximum possible time for the particle to hit the ground.