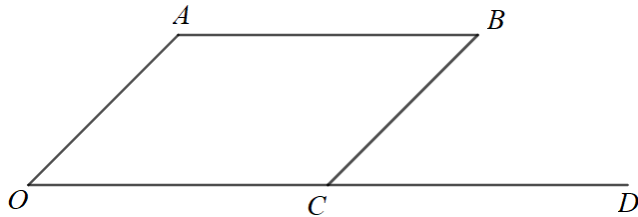


Vectors in Geometry - www.m4ths.com

(1) The diagram below shows the parallelogram $OABC$.



$\vec{OA} = a$, $\vec{AB} = b$ and $OC = CD$

X lies on OA such that $OX:XA$ is $2:1$ and Y is the midpoint of AB .

(a) Find the following vectors in terms of a and b fully simplifying your answers.

- (i) \vec{OB} (ii) \vec{AO} (iii) \vec{OC} (iv) \vec{BC} (v) \vec{OD} (vi) \vec{BD}
 (vii) \vec{BA} (viii) \vec{CO}

(b) Find the following vectors in terms of a and b fully simplifying your answers.

- (i) \vec{OX} (ii) \vec{AY} (iii) \vec{OY} (iv) \vec{BX} (v) \vec{XY} (vi) \vec{YX}

(c) Prove that \vec{XC} is NOT parallel to \vec{YD}

The point Z is the midpoint of BC

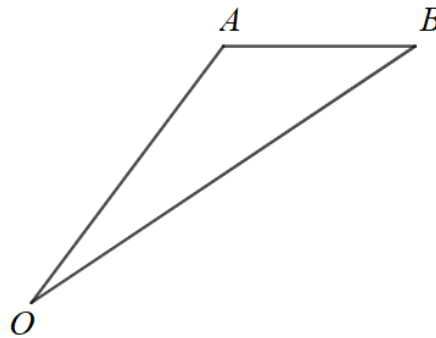
(d) Prove that AZD is a straight line.

(e) Explain why the points A, Z and D are collinear.

N is the midpoint of CD

(f) Show that \vec{YC} and $-\vec{NB}$

(2) The diagram below shows the triangle OAB .



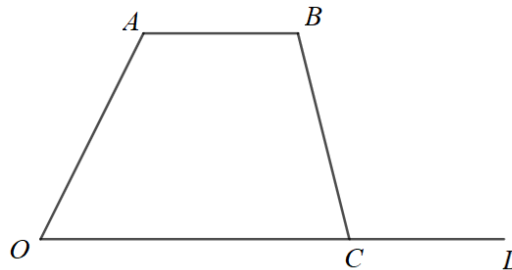
$\vec{OA} = 3p + 4q$ and $\vec{OB} = 6p + 4q$

(a) Show that \vec{AB} can be written in the form kp .

The point X is the midpoint of OB .

(b) Show that \vec{AX} can be written in the form nq .

(3) The diagram below shows that trapezium $OABC$.



$\vec{OA} = a$, $\vec{AB} = b$, $AB = CD$ and the ratio $OC:CD$ is $2:1$

(a) Find the following vectors in terms of a and b fully simplifying your answers.

- (i) \vec{OB} (ii) \vec{AO} (iii) \vec{OC} (iv) \vec{BC} (v) \vec{OD} (vi) \vec{BD}
 (vii) \vec{BA} (viii) \vec{CO}

The point X is the midpoint of OC .

(b) Show that \vec{OA} and \vec{BX} are a parallel.

The point Y lies on the line OC such that $OY:YC$ is $5:1$

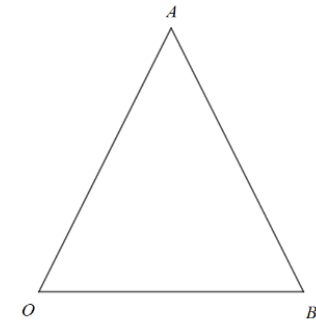
(c) Prove that \vec{AY} and \vec{BD} are a not parallel.

The point P is the midpoint of OA and the point Q is the midpoint of BC .

(d) Show that \vec{OD} and \vec{PQ} are a parallel.

(e) Find the ratio $PQ:OD$

(4) The diagram below shows the triangle OAB .



$\vec{OA} = 4p + 8q$, $\vec{OB} = 8p$

The point X is the midpoint of OB .

The point Y lies on OB such that $OY:YB$ is $3:1$

The point Z lies on OA such that $OZ:ZA$ is $3:1$

The point T is the midpoint AX

(a) Prove that ZTY is a straight line

(b) Find the ratio $ZT:TY$