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(1) (a) Show that $(x + 2)(x + 4) \equiv x^2 + 6x + 8$

(b) Hence, show that $(x + 2)(x + 4)(x + 1) \equiv x^3 + 7x^2 + 14x + 8$

(2) Show that $(x + 1)(x + 3)(x + 5) \equiv x^3 + 9x^2 + 23x + 15$

(3) Show that $(x - 2)(x + 1)(x + 3) \equiv x^3 + 2x^2 - 5x - 6$

(4) Expand and simplify each of the following:

(a) $(x + 6)(x + 2)(x + 1)$ (b) $(x - 1)(x - 2)(x + 5)$

(c) $(x - 5)(x - 3)(x - 4)$ (d) $(x + 1)(x - 1)(7 - x)$

(5) Show that $(2x - 3)(x + 1)(x - 2) \equiv 2x^3 - 5x^2 - x + 6$

(6) Expand and simplify each of the following:

(a) $(3x + 1)(x + 3)(x + 1)$ (b) $(2x - 1)(x - 1)(x + 8)$

(c) $(x - 5)(4x - 3)(x + 2)$ (d) $(3x + 2)(2x - 3)(4 - x)$

(7) Expand and simplify $x(3 - x)(4 + x)$

(8) Expand and simplify $(x + 3)^2(x - 4)$

(9) Expand and simplify $(3x - 2)^3$

(10) Write down the solutions to each of the following cubic equations:

(a) $(x + 3)(x - 2)(x + 7) = 0$ (b) $x(x - 3)(x + 10) = 0$

(c) $(x - 1)(3x - 5)(x - 6) = 0$ (d) $(2x + 1)(1 - x)(3x + 7) = 0$

(11) (a) Show that $(4x - 1)(3x + 1)(x + 2) \equiv 12x^3 + 25x^2 + x - a$ where a is a constant to be found.

(b) Hence, solve the equation $12x^3 + 25x^2 + x = a$

(12) Show that

$$(x - 1)(x + 3)(x + 2) - (x + 3)(x - 3)(x + 1) \equiv (3x + 1)(x + 3)$$

(13) Show that $(x + 1)^3 + (x - 1)^3 \equiv Ax(x^2 + B)$ where A and B are constants.

(14) Expand and simplify $(1 - x)^2(1 + x)^2$

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(6) Expand and simplify each of the following:

(a) $(3x + 1)(x + 3)(x + 1)$ (b) $(2x - 1)(x - 1)(x + 8)$

(c) $(x - 5)(4x - 3)(x + 2)$ (d) $(3x + 2)(2x - 3)(4 - x)$

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$$(x - 1)(x + 3)(x + 2) - (x + 3)(x - 3)(x + 1) \equiv (3x + 1)(x + 3)$$

(13) Show that $(x + 1)^3 + (x - 1)^3 \equiv Ax(x^2 + B)$ where A and B are constants.

(14) Expand and simplify $(1 - x)^2(1 + x)^2$