

Chapter 2 Test – FM1 – Work, Energy & Power – www.m4ths.com

(Take $g = 9.8\text{ms}^{-2}$ when not exact)

(1) A particle of mass 0.5kg is dropped from a height of h and hits the floor with speed $v\text{ms}^{-1}$. The particle experiences constant resistance of 4N from air resistance throughout its motion.

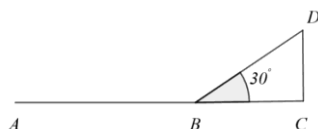
(a) Explain why you would not use the principle of the *Conservation of Mechanical Energy* for this question.

(b) Show that v satisfies the equation $v = \sqrt{2h(g - 8)}$

(c) State one criticism with the model.

(2) A small toy car of mass 2kg moves along a rough horizontal surface. The engine of the car is working a constant rate of 600W . The coefficient of friction between the car and the surface is 0.25 . The car also experiences an **additional** constant resistance of 10N independent of friction. Show that the maximum speed of the car doesn't exceed 41ms^{-1} .

(3) A boy pedals his bike from rest from the point D to B where $DB = 40\text{m}$. He then continues to the point A where $AB = 100\text{m}$ as shown in the diagram below.



You can assume that ABC is a straight horizontal road and that DC is perpendicular to AC .

The boy and his bike have a combined mass of 80kg and the boy is pedalling with a constant pedalling force from point D to point A . The boy experiences constant resistance of 100N throughout the journey. Given that his speed is 10ms^{-1} when he reaches A , find the pedalling force the boy produces.

(4) A particle of mass 4kg is pulled up the greatest slope of a rough plane inclined at an angle θ where $\tan \theta = \frac{5}{12}$ by a constant force $X\text{N}$. The coefficient of friction between the particle and the plane is μ . The initial speed of the particle is 2ms^{-1} and after the particle has travelled a distance of d metres the speed of the particles has halved.

(a) Show, using the *Work-Energy Principle*, that μ satisfies the equation $\mu = \frac{d(13X - 20g) + 78}{48gd}$

(b) When $d = 10$ show that $\frac{941}{65} < X \leq \frac{3293}{65}$ giving a justification for your answer.

(5) A model van of mass 10kg is travelling down a rough straight road inclined at an angle of α to the horizontal when $\tan \alpha = 0.1$ with a constant speed of 6ms^{-1} . The engine of the van is working at a rate of 2kW and experiences constant resistances to motion of $X\text{N}$ which act parallel to the road.

(a) Find the value of X to 3S.F.

The van now increases the rate at which the engine is working to 3kW . Given that the resistances experienced by the van don't change

(b) Find the initial acceleration of the van.