

Averages from Tables

Answers www.maths.com

① a) Should divide by sum of frequency which is 20, not 4.

$$\begin{aligned} \text{b) } & \frac{(2 \times 0) + (13 \times 1) + (4 \times 2) + (1 \times 3)}{20} \\ &= \frac{0 + 13 + 8 + 3}{20} \\ &= \frac{24}{20} \\ &= 1.2 \checkmark \end{aligned}$$

⑤ The mode is 1 with a frequency of 13.

a) 1

⑥ The range is 3 (3-0). Fred has done the range of the frequency.

b) $3 - 0 = 3$. This is the range of phones owned by people.

$$\begin{aligned} \text{⑦ } & \frac{(23 \times 0) + (5 \times 1) + (1 \times 2) + (0 \times 3) + (1 \times 4) + (0 \times 5)}{30} \\ &= 0 + 5 + 2 + 0 + 4 + 0 \\ &= \frac{11}{30} \text{ or } 0.36 \text{ which is } 0.37 \text{ bp.} \end{aligned}$$

$$\begin{aligned} \text{③ } & \frac{2+2+12+10+6+91+64+27+10}{35} \\ &= 6.4 \end{aligned}$$

④ Grouped data. We don't know the exact value of each height.

⑥ Yes he is correct

$$\text{c) } \frac{158}{17} = 9.29 \text{ to 2dp.}$$

⑦ The smallest could be 6cm and the tallest 10cm which gives a range of 4cm $\therefore 5\text{cm}$ could be correct.

$$\text{⑤ } \frac{(5 \times 1) + (12 \times 4) + (10 \times 8) + (3 \times 15)}{30}$$

$$= \frac{5 + 48 + 80 + 45}{30}$$

$$= \frac{178}{30} \text{ or } 5.93$$

⑥ Grouped data means we don't know the exact time spent by each student.

⑦ 30 students

The median will be in the second class as $\frac{30}{2} = 15$. The second class is $2 < N \leq 6$. \therefore median between 2 and 6 not 0.5.

⑧ Increase as $7 > 5.93$

$$\textcircled{6} \textcircled{a} \frac{(12 \times 90) + (3 \times 110) + (7 \times 140)}{22}$$

$$= 108.6 \text{ to } 1 \text{ dp.}$$

$$\textcircled{6} 160 - 80 = 80 \text{ cm}$$

\textcircled{c} Median using interpolation:

$$\frac{22}{2} \therefore 11^{\text{th}} \text{ data item}$$

The median will be in the interval $80 \leq h < 100$ and could have been 92.

\textcircled{7} \textcircled{a} FF CCCT

\textcircled{b} Small number of observations where data has large spread.

The likelihood of multiple values being the same is low given (t) is to the second.

\textcircled{c} No outliers and units are time

$$\textcircled{8} \textcircled{a} \frac{21}{2} = 11.5^{\text{th}} \text{ value.}$$

Using CF: 6, 8, 14, 21, 21

$$60 + \left(\frac{3.5}{6}\right) \times 10 = 65.8$$

$$\textcircled{b} 80 - 49 = 31$$

$$\textcircled{c} \{x < 40\} \cup \{x \geq 80\}$$

$$\textcircled{d} \frac{270 + 110 + 390 + 525}{21} = 61.7$$

\textcircled{a} The mode is 0, The mean will have to have a value greater than 0 as 7 people have an average greater than 0.

\textcircled{b} Median will be in the same class interval as mode as $\frac{20}{2} = 10.5$ and there are 13 in the class

$$\textcircled{c} \frac{(13 \times 0) + (2 \times 1) + (7 \times 4)}{20} = 1.5$$

$$\textcircled{d} 2 - 0 = 2$$

\textcircled{e} let the missing values be x and y and use simultaneous equations:

$$2x + y = 10 \quad (\text{based on SF}) \quad \textcircled{1}$$

$$\frac{3 + 2x + 3y + 20 + 15}{32} = 2$$

$$2x + 3y = 26 \quad (\text{based on mean}) \quad \textcircled{2}$$

$$\begin{aligned} 2x + 3y &= 26 \\ 2x + 2y &= 20 \end{aligned} \quad \therefore y = 6 \text{ and } x = 4$$

4 goes in the frequency for 2

6 goes in the frequency for 3

	#	Frequency
0	0	
1	0	
2	1	
3	2	
4	3	
5	25	

	#	
0	24	✓ median
1	0	= 0
2	0	
3	1	
4	2	
5	3	

$$\textcircled{12} \frac{30 + \left(\frac{10+y}{2}\right) \times 8 + \left(\frac{y+40}{2}\right) \times 4 + 90}{20} = 15.6$$

$$\therefore y = 12 \Rightarrow 10 + \left(\frac{4.5}{8}\right) \times 1 = 10.5625$$