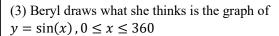
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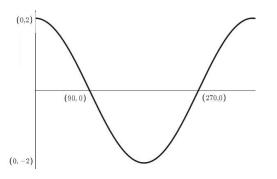
(49) Sine, Cosine & Tangent Graphs

WORKING AT D/E

(1) On separate sets of axes, sketch the graphs of: (i) y = cos(x), $0 \le x \le 360$ (ii) y = sin(x), $0 \le x \le 360$ (iii) y = tan(x), $0 \le x \le 360$ For each graph, show where the curve meets the coordinate axes, any maximum or minimum points and the equations of any asymptotes.

(2) Complete the following sentences: The graph of $y = \sin(x)$ cycles every_____ The graph of $y = \tan(x)$ cycles every_____ The graph of $y = \cos(x)$ cycles every_____





WORKING AT B/C

(1) On separate sets of axes, sketch the graphs of: (i) $y = \cos(x)$, $-360 \le x \le 360$ (ii) $y = \sin(x)$, $-360 \le x \le 360$ (iii) $y = \tan(x)$, $-360 \le x \le 360$ For each graph, show where the curve meets the coordinate axes, any maximum or minimum points and the equations of any asymptotes.

(2) (a) On the graph of $y = \sin(x)$, $0 \le x \le 360$, $y = \frac{\sqrt{3}}{2}$ when $x = 60^{\circ}$. Where else on the graph will $y = \frac{\sqrt{3}}{2}$? (b) On the graph of $y = \cos(x)$, $0 \le x \le 360$,

y = 0 when $x = 90^{\circ}$. Where else on the graph will y = 0?

(c) On the graph of $y = \tan(x)$, $0 \le x \le 540$, y = 1 when $x = 45^{\circ}$. Where else on the graph will y = 1?

(3) Write down any lines of symmetry for each graph (i) $y = \cos(x)$, -360 < x < 360(ii) $y = \sin(x)$, -180 < x < 180(iii) $y = \tan(x)$, -360 < x < 360

WORKING AT A*/A

(1) By considering the graphs of *sin*, *cos* and *tan*, tick any of the following statements that are true:

1.
$$\sin(x) \equiv \sin(180 - x)$$

2. $\sin(x) \equiv \sin(180 + x)$
3. $\cos(x) = \cos(360 + x)$
4. $\sin(x) \equiv \sin(360 + x)$
5. $\tan(x) = \tan(360 + x)$
6. $\cos(360 - x) = \cos(x)$
7. $\tan(x) = \tan(180 + x)$
8. $\sin(-x) \equiv -\sin(x)$
9. $\cos(x) \equiv \sin(90 - x)$
10. $\tan(-x) = -\tan(x)$
11. $\cos(x) \equiv \cos(180 + x)$
12. $\cos(x) = \cos(-x)$

(2) Find all of values of x given 0 < x < 360 for (a) $\tan(x) = -1$ (b) $\sin(x) = -\frac{\sqrt{3}}{2}$ (c) $\cos(x) = \frac{1}{\sqrt{2}}$ (d) $\cos(x) = -0.1$ (e) $\tan(x)$ is undefined. (f) $\sin(x) = -\frac{\sqrt{5}}{2}$

(3) How many points of intersection are there between each pair of graphs for $0 \le x \le 360$? (a) $y = \cos(x)$ and $y = \sin(x)$ (b) $y = \cos(x)$ and $y = \tan(x)$ (c) $y = \tan(x)$ and $y = \sin(x)$

Write down two errors with she has made.

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