

## WORKING AT B/C

(1) (a) Given that 2n is always even, show that the sum of the squares of two consecutive even numbers can be written as

 $8n^2 + 8n + 4$ 

(b) Hence, prove that the sum of the squares of two consecutive even numbers is always divisible by 4.

## WORKING AT A\*/A

(1) Prove, that if *a* and *b* are both positive numbers, then  $\frac{a^2+b^2}{2a} \ge 1$ 

(2) If n is a single digit odd number, prove that n + 1 is not always a single digit even number.

(2) Prove that the difference between the cubes of any consecutive integers is always one more than a multiple of 3.

(2) Prove, that is x and y are both positive integers, then  $\frac{y}{x} + \frac{x}{y} \ge 2$ 

(3) Prove, by counter example, that  $2n^2 + 1$  for all positive integers *n* is not always a prime number.

A Level Maths Year 1 Pure - Steve Blades 2023-2024 © - Full worked solutions are available at www.m4ths.com