

## (22) Binomial Expansion of the form $(a + bx)^n$

### WORKING AT D/E

(1) (a) Show that  $(4 + x)^{\frac{1}{2}}$  can be written as

$$2 \left( x + \frac{x}{4} \right)^{\frac{1}{2}}$$

(b) Hence, using the formula book, find the first 3 terms in the expansion of  $(4 + x)^{\frac{1}{2}}$

(c) Write down the set of values of  $x$  for which the expansion is valid.

(2) (a) Cyril wants to find the expansion of  $(3 - x)^{-2}$ . He wants to use Pascal's Triangle to find the coefficients of each term. Explain why he can't

(b) Using the formula book, show that the first 3 terms in ascending powers of  $x$  in the expansion of  $(3 - x)^{-2}$  are  $\frac{1}{9} + \frac{2}{27}x + \frac{1}{27}x^2 \dots$

(c) Write down the set of values of  $x$  for which the expansion is valid.

(3) Find the first 4 terms in ascending powers of  $x$  in the expansion of  $(2 + 3x)^{-4}$ ,  $|x| < \frac{2}{3}$

### WORKING AT B/C

(1) Use the formula book to show that the first 3 terms in ascending powers of  $x$  in the expansion of  $\frac{1+x}{\sqrt{9-x}}$ ,  $|x| < 9$  are  $\frac{1}{3} + \frac{19}{54}x + \frac{13}{648}x^2 \dots$

(2) (a) Find the first 3 terms in the expansion of  $\sqrt{2+x}$ ,  $|x| < 2$  in ascending powers of  $x$  simplifying each coefficient.

(b) Use your answer to part (a) with a suitable value of  $x$  to find an approximation to value of  $\frac{\sqrt{201}}{10}$

(3) Find the first 2 terms in the series expansion of  $\frac{5-x}{(2+x)^2}$  stating the set of values of  $x$  for which the expansion is valid.

### WORKING AT A\*/A

(1)  $f(x) = (2 + bx)^c$

Given that the first two terms in the binomial expansion of  $f(x)$  are  $\frac{1}{4} - \frac{3}{4}x \dots$

(a) Write down the value of  $c$

(b) Find the value of  $b$ .

(c) Find the 3<sup>rd</sup> term in the expansion

(d) Find the set of values of  $x$  for which the expansion is valid.

(e) Without any further expansions, find the first 3 terms in the expansion of  $(2 - bx)^c$

(2) (a) Find the first 4 terms in ascending powers of  $x$  in the expansion of  $(x + 8)^{\frac{1}{3}}$  simplifying each term.

(b) Find the set of values of  $x$  for which the expansion is valid.

(c) Use your answer to part (b) to find a cubic approximation for  $\sqrt[3]{9}$ , showing all your workings.

(d) Find the percentage error in your approximation.

(e) Explain how this approximation could be improved.

(3) (a)  $h(x) = \frac{1}{1+x} + \frac{1}{1-x}$ ,  $|x| < 1$

Explain why there are no odd powers of  $x$  in the series expansion of  $h(x)$ .