

## (19) Recurrence Relations and Periodic Sequences

### WORKING AT D/E

(1)  $u_{n+1} = 4u_n - 1, u_1 = 3.$

(a) Find  $u_2, u_3$  and  $u_4.$

(b) Explain why the sequence is not arithmetic.

(c) Find

$$\sum_{r=1}^5 u_r$$

(2)  $u_{n+1} = -u_n, u_1 = 4.$

(a) Find  $u_2, u_3$  and  $u_4.$

(b) Name what type of sequence this is.

(c) Explain why

$$\sum_{r=1}^{2000} u_r = 0$$

### WORKING AT B/C

(1)  $u_n = \cos(90n^\circ), n \geq 1$

(a) Show that the order of the sequence is 4

(b) Explain why

$$\sum_{r=1}^{4n+2} u_r = -1$$

(2)  $u_{n+1} = (u_n)^2 - 1, u_1 = p, p > 0$

(a) Find an expression for  $u_2,$

Given that

$$\sum_{r=1}^2 u_r = 19$$

(b) Find the value of  $p$

(3)  $u_n = (-1)^n, n \geq 1$

(a) Show that the sequence is periodic and state its period.

(b) Write down the value of

$$\sum_{r=1}^{8001} u_r$$

### WORKING AT A\*/A

(1) A sequence is defined for  $n \geq 2$  by the recurrence relation

$$u_n = u_{n-1} - 3, u_1 = k,$$

(a) Show that the sequence is arithmetic.

Given that  $u_8 = -11$

(b) Find the value of  $k$

(c) Evaluate

$$\sum_{r=1}^{40} u_r$$

(2)  $u_n = \tan(180n^\circ) + \cos(180n^\circ), n \geq 1$

Explain why

(a)

$$\sum_{r=1}^{2n} u_r = 0$$

(b)

$$\sum_{r=1}^{2n+1} u_r = -1$$