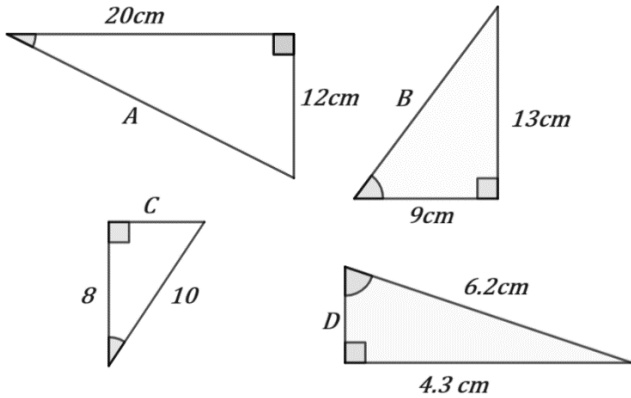
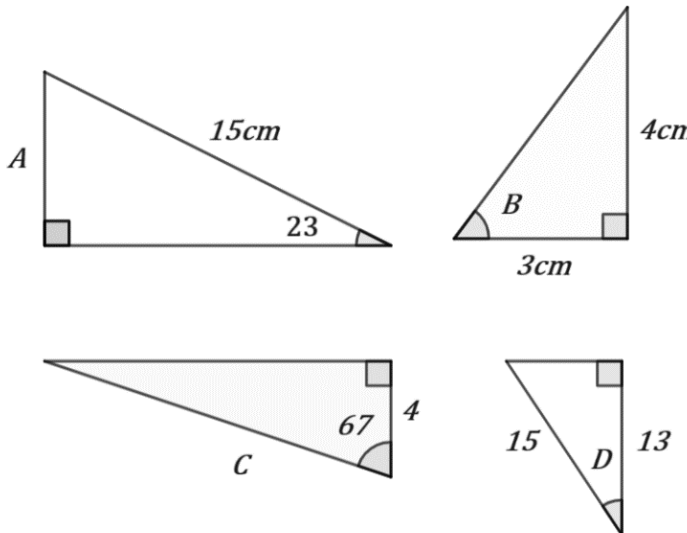


3D Trigonometry and Pythagoras Theorem
 www.m4ths.com – Steve Blades ©

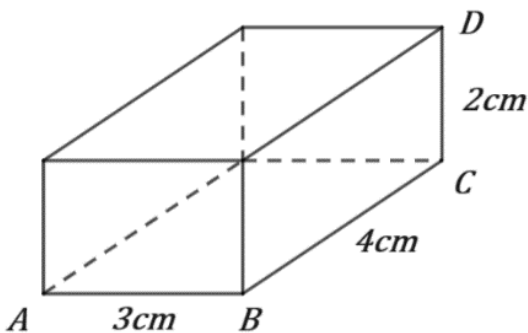
(1) Find the missing values in the triangles. Give any non-integer answers to 3 SF.



(2) Find the missing values in the triangles. Give any non-integer answers to 3SF.

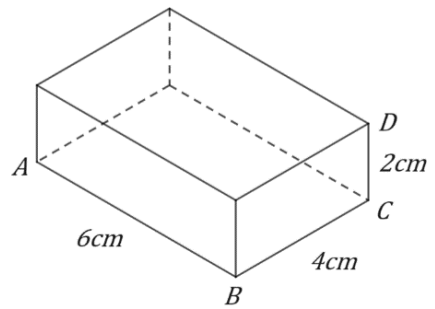


(3) A cuboid is shown below.



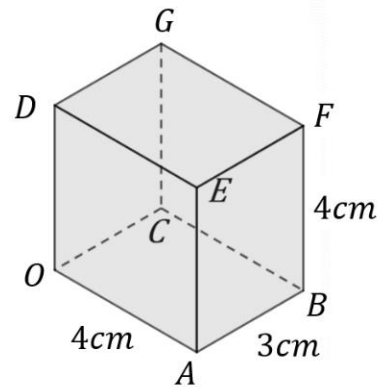
- (a) Draw the 2D triangle ABC and show that $AC = 5\text{cm}$.
- (b) Draw the 2D triangle DAC and show that $AD = \sqrt{29}$
- (c) Using your answers to part (a) and (b), find the size of $\angle DAC$ to 3 significant figures.
- (d) On the diagram, draw all lines that have length $\sqrt{29}$.

(4) The diagram below shows a cuboid.



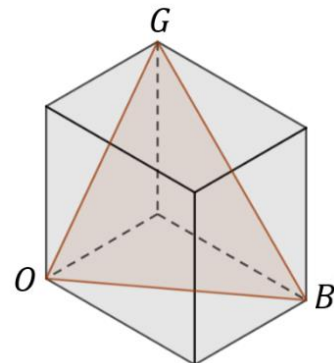
- (a) Use Pythagoras Theorem in 3D to show that the length on the diagonal $AD = 2\sqrt{14}\text{cm}$ long.
- (b) On the diagram mark the vertex E such that the length $BE = 2\sqrt{14}$.
- (c) Show that $AC = 2\sqrt{13}\text{cm}$ long
- (d) Draw the right-angled triangle ACD showing the lengths of AC and DC on your diagram.
- (e) Hence, using trigonometry in 3D, show that the angle $DAC = 15.5^\circ$ correct to 3 significant figures.

(5) The diagram below shows a cuboid $OABCDEFG$.



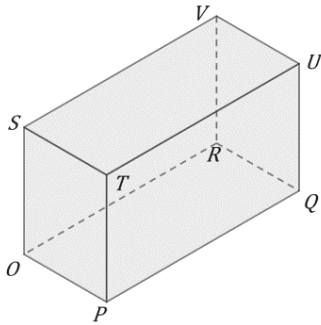
- (a) Show that $OB = 5\text{cm}$.
- (b) Hence or otherwise, show that $OF = \sqrt{41}$.
- (c) Explain why AG also has length $\sqrt{41}$.
- (d) Find the size of $\angle FOB$ using the answers you have found previously.
- (e) Find another angle that has the same size as $\angle FOB$.

The triangle OBG is drawn within the cuboid $OABCDEFG$ as shown below.



- (f) Show that $\triangle OBG$ is an isosceles triangle.
- (g) Find the size of $\angle OBG$.
- (h) Find the area of $\triangle OBG$.

(6) The diagram below shows a cuboid $OPQRSTUV$.



Given that $UQ = 6\text{cm}$ and $\angle UOQ = 30^\circ$ find:

(a) OU (b) OQ (c) VP (d) OS

Given further that $OP = 5\text{cm}$:

(e) Find the volume of the cuboid.

(f) Find the area of $\triangle VPR$.

X is the midpoint of the line SV .

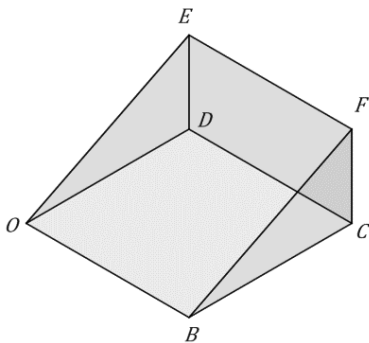
(g) Find the area of the triangle PQX .

Point Y lies on VR such that $RY:YV$ is 2:1.

(h) Find the size of $\angle YPR$.

(7) The diagram below shows a 'right wedge'

$BC = 8\text{cm}$, $\angle FCB = 90^\circ$, $\angle EOD = 90^\circ$ & $\angle FBC = 24^\circ$



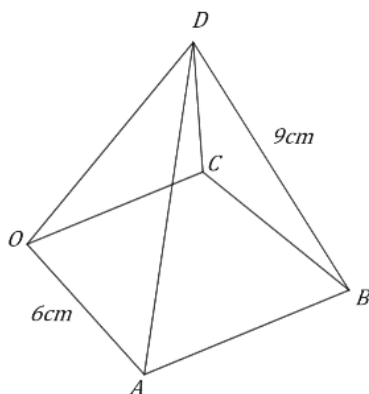
(a) Find the length BF .

(b) Hence write down the length OE .

(c) Find OC .

(d) Find $\angle FOC$.

(8) The diagram shows a square based pyramid $OABD$ where point D is directly above the centre of the base.



(a) Show that the perpendicular height of the pyramid is $3\sqrt{7}\text{cm}$ long.

(b) Hence, find the volume of the pyramid.

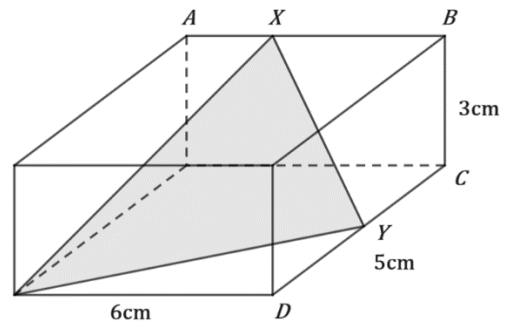
(c) Find the size of $\angle DOB$.

(d) Find the total surface area of the solid pyramid.

(9) A cube has side length a .

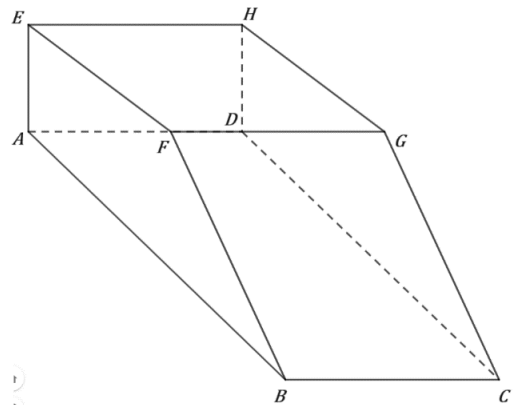
Find a simplified expression in terms of a for the length of the longest diagonal in the cube

(10)* The diagram below shows a cuboid.



Given that $AX:XB = 1:2$ and $AY:YC = 1:1$ find the area of the shaded triangle.

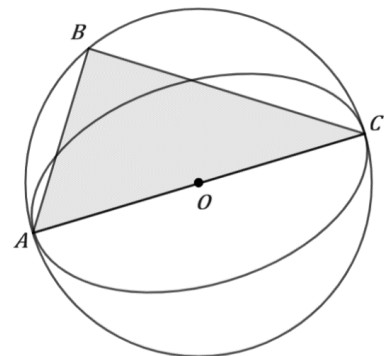
(11) The diagram below shows a 'right wedge' or, if you like a 'trapezoidal prism'.



$\angle BAC = \angle AEF = \angle BAD = \angle ABC = \angle BCD = 90^\circ$
 $AB = 12$, $BF = 7$ and $AF = 6$

Find the volume of the prism to 3SF.

(12) The diagram below shows a sphere centre O , and diameter AB . Point C touches the outer of the sphere and $\triangle ABC$ is a right-angled triangle.



Given that $AB = 2x$ and that $\tan \angle BCA = \frac{1}{\sqrt{3}}$, without a calculator, show that the volume of the sphere is $\frac{32x^3\pi}{3}$