

Quadratic Functions

(1) Factorise the following quadratic expressions:

- (a) $x^2 - x - 12$
- (b) $8 - 6x + x^2$
- (c) $x^2 + 3x$

(2) Solve the following quadratic equations:

- (a) $(x-2)(x+1) = 0$
- (b) $(2x+3)(x+4) = 0$
- (c) $x^2 - 2x - 8 = 0$
- (d) $x(x-1) = 6$

(3) Factorise the following quadratic expressions:

- (a) $2x^2 + x - 1$
- (b) $3x^2 - 5x - 2$
- (c) $12x^2 + 16x - 3$

(4) Factorise and solve the following quadratic equations:

- (a) $2x^2 - 5x - 3 = 0$
- (b) $5x^2 + 4x - 1 = 0$
- (c) $6x^2 + 7x = 3$
- (d) $x(2x-1) = 15$
- (e) $0.4x^2 + x = 0.6$

(5) (a) Given that the quadratic equation $f(x) = (2x-3)(3x-5)$ can be written in the form

$f(x) = ax^2 + bx + c$, find the values of a, b and c .

(b) Write down the solutions to the equation $f(x) = 0$.

(c) Find the solutions to the equation $f(x) = 15$.

(6) Write the following quadratic expressions in the form $(x+a)^2 + b$

- (a) $x^2 - 4x - 3$
- (b) $2 - 6x + x^2$
- (c) $x^2 + 5x + 2$
- (d) $x^2 + 3x$

(7) Solve the following quadratic equations by completing the square leaving

your answers in exact form where appropriate:

- (a) $x^2 - 2x - 8 = 0$
- (b) $x^2 + 3x + 1 = 0$
- (c) $x^2 + 8x = 12$
- (d) $2x^2 + 7x - 1 = 0$

(8) Write the following quadratic expressions in the form $a(x+b)^2 + c$:

- (a) $2x^2 + 4x + 7$
- (b) $-x^2 + 5x - 2$
- (c) $7x^2 + 3x + 1$
- (d) $8x + 5x^2$

(9) Solve the following quadratic equations by completing the square leaving your answers in exact form where appropriate:

- (a) $3x^2 + 6x - 1 = 0$
- (b) $7x^2 + 5x - 2 = 0$
- (c) $4x(x-6) = 7$

(10) (a) Sketch the graph of $y = x^2 + 4x + 1$ showing any points of intersection with the coordinate axes and the coordinates of the minimum point.

(b) Sketch the graph of $y = 2x^2 + 5x - 4$ showing any points of intersection with the coordinate axes and the coordinates of the minimum point.

(c) Sketch the graph of $y = 3 - 5x - x^2$ showing any points of intersection with the coordinate axes and the coordinates of the maximum point.

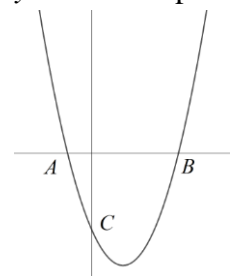
(11) (a) Given that the quadratic expression $2(x+0.75)^2 - 1$ can be written in the form $ax^2 + bx + c$. Find the values of a, b and c .

(b) Solve the equation $2(x+0.75)^2 - 1 = 0$ giving your answers in exact form.

(12) Use the quadratic formula to find the solutions to the following equations. Give your answers in exact form:

- (a) $x^2 - 3x - 8 = 0$
- (b) $0 = 2 - 10x + x^2$
- (c) $3x^2 - 2x - 4 = 0$
- (d) $-x^2 + 7x - 1 = 0$
- (e) $7x^2 = 1 + 5x$
- (f) $0.3x + 1.2x^2 - 2.5 = 0$

(13) Part of the graph of $y = 4x^2 - 12x - 19$ is shown below. The curve crosses the x axis at the points A and B and the y axis at the point C .



- (a) Write down the coordinates of the point C .
- (b) Find the length of the line segment AB giving your answer in exact form.

(14) In completed square form the equation $y = x^2 + px + q$ can be written as $y = (x-2)^2 - 5$

- (a) Find the values of p and q .
- (b) Sketch the graph of $y = (x-2)^2 - 5$ showing any point of intersection with the coordinate axes.
- (c) Label the minimum point M on the graph and write down its coordinates.
- (d) The graph crosses the x axis at the points A and B . Find the area of the triangle AMB giving your answer in exact form.

(15) (a) Find the solutions to the equation $px^2 + qx + r = 0$ in terms of p, q and r .

(b) Given that $p < 0 < r < q$ draw a rough sketch of the curve $y = px^2 + qx + r$