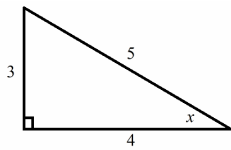


**www.m4ths.com – C2 –
Trigonometry (1)**

(1) Using the triangle below, show that:

(a) $\frac{\sin x}{\cos x} = \tan x$

(b) $\sin^2 x + \cos^2 x = 1$



(2) Simplify the following expressions:

(a) $\frac{\sin 3\theta}{\cos 3\theta}$

(b) $4\sin^2 2x + 4\cos^2 2x$

(c) $3 - 3\cos^2 5x$

(d) $\frac{3\sin^2 4p}{\sin 4p\sqrt{1-\sin^2 4p}}$

(3) Show the expression $(\sin x + \cos x)^2 - (\sin x - \cos x)^2$ can be written as $k \sin x \cos x$ stating the value of k .

(4) Prove the following identities:

(a) $\frac{\sin^2 x - \cos^2 x}{\sin x + \cos x} \equiv \sin x - \cos x$

(b) $\frac{\sqrt{1-\cos^2 3x}}{\sqrt{1-\sin^2 3x}} \equiv \tan 3x$

(c) $\sin^4 x - \cos^4 x \equiv 1 - 2\cos^2 x$

(d) $\frac{\cos x}{\sin x} + \frac{\sin x}{\cos x} \equiv \frac{1}{\sin x \cos x}$

(5) Given $\sin A = \frac{3}{5}$ and that A is obtuse, find the values of:

(a) $\cos A$

(b) $\tan A$

(6) Given $x = 3\cos A$ and $y = 2\sin A$, write an equation connecting y and x .

Give all answers to 1 decimal place where appropriate.

(7) Solve the following equations in the interval $0 \leq x \leq 360^\circ$:

(a) $\sin x = 0.5$

(b) $\cos x = \frac{1}{\sqrt{2}}$

(c) $\tan x = 1$

(d) $\cos x = \frac{\sqrt{3}}{2}$

(e) $\sin x = -\frac{\sqrt{3}}{2}$

(8) Solve the following equations in the interval $0 \leq x \leq 2\pi$ giving your answers as multiples of π :

(a) $\sin x = \frac{\sqrt{3}}{2}$

(b) $\tan x = \frac{1}{\sqrt{3}}$

(c) $\cos x = -\frac{1}{2}$

(d) $\tan x = -1$

(9) Solve the following equations for $0 \leq x \leq 360^\circ$:

(a) $\sin x = 0.24$

(b) $\cos x = 0.83$

(c) $3 \tan x - 1 = 2.12$

(d) $4 \sin x = -1.08$

(10) Solve the following equations for $0 \leq x \leq 2\pi$:

(a) $\cos x = -0.54$

(b) $\tan x = 3.7$

(c) $1 - \sin x = 0.43$

(d) $2 \cos x = \sin x$

(11) Solve the following equations in the interval $-180^\circ \leq x \leq 180^\circ$:

(a) $\sin(x - 30^\circ) = \frac{\sqrt{3}}{2}$

(b) $\cos(x + 45^\circ) = \frac{1}{2}$

(c) $3 \tan(x - 15^\circ) = \sqrt{3}$

(d) $2 \sin(x + 60^\circ) = \sqrt{2}$

(12) Solve the following equations in the interval $0 \leq x \leq 2\pi$:

(a) $2 \cos\left(x + \frac{\pi}{3}\right) = \sqrt{3}$

(b) $\tan\left(x - \frac{\pi}{4}\right) = \frac{1}{\sqrt{3}}$

(13) Solve the following equations for $0 \leq x \leq 180^\circ$.

(a) $\sin(3x) = \frac{\sqrt{3}}{2}$

(b) $\cos(2x) = 0.45$

(c) $\sin(3x - 20^\circ) = 0.3$

(d) $\tan(2x + 12^\circ) = 1.3$

(14) Solve the following equations the interval $0 \leq x \leq \pi$

(a) $\tan(3x - 1.2^\circ) = 0.4$

(b) $\sin(2x - 0.2^\circ) = -0.12$

(c) $2 \cos(3x + 0.65^\circ) = 1.87$

(15) Solve the following equations in the interval $0 \leq x \leq 360^\circ$:

(a) $2 \sin x = \sin x \cos x$

(b) $\sin(2x - 10^\circ) = \sin(50^\circ)$

(c) $\tan(3\theta - 20^\circ) = \tan(30^\circ)$

(16) Solve the following equations for $0 \leq x \leq 360^\circ$:

(a) $\sin^2 x = \frac{1}{2}$

(b) $\tan^2 2x = 1$

(c) $2 \sin^2 x - \sin x = 1$

(d) $(\cos x - 1)(2 \sin x - 1) = 0$

(e) $4 \sin^2 x - 4 \cos x - 1 = 0$

(f) $2 \cos \frac{1}{2} x = \tan \frac{1}{2} x$

(17) Solve the following equations for $0 \leq x \leq 2\pi$:

(a) $\cos^2 x - \sin\left(\frac{\pi}{2} - x\right) = 2$

(b) $3 \tan^2 x + 5 \tan x - 2 = 0$

(c) $\sin x(2 \sin x + 1) = 0$

**www.m4ths.com – C2 –
Trigonometry (2)**

(1) Solve the equation
 $2 \cos^2 x - 9 \sin x + 3 = 0$
in the interval $0 < x \leq 2\pi$ giving
your answers as multiples of π .

(2) (a) Show the equation
 $2 \cos x + 3 \sin x = 0$ can be
written as $\tan x = -\frac{2}{3}$.

(b) Hence or otherwise solve
the equation

$$2 \cos \frac{\theta}{2} + 3 \sin \frac{\theta}{2} = 0$$

in the interval $0 \leq \theta \leq 360^\circ$
giving your answer to 3
significant figures.

(3) (a) If $x = 3 \cos \theta - 1$ and
 $y = 3 \sin \theta + 2$ show that

$$(x+1)^2 + (y-2)^2 = r^2$$

stating the value of r .

(b) Sketch the graph of

$$(x+1)^2 + (y-2)^2 = r^2$$

showing
any points of intersection with
the coordinate axis in exact
form.

(4) Show that the equation

$2 \sin x = 3 \tan x$ has 2 solutions
in the interval $0 < x \leq 2\pi$ giving
the solutions as multiples of π .

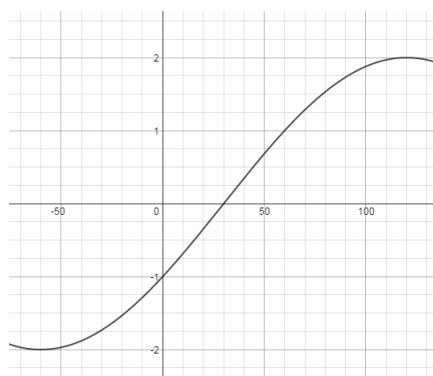
(5) The graph below shows part
of the curve $y = p \sin(x - q^\circ)$.

(a) Write down the values
of p and q .

(b) Solve the equation

$$p \sin(x - q^\circ) = \sqrt{3}$$

in the interval $0 \leq x \leq 360^\circ$.



(6) (a) Show the expression
 $\sin^4 x - \cos^4 x$ can be written in
the form $a \sin^2 x - 1$ stating the
value of a .

(b) Hence or otherwise solve
the equation

$$\sin^4 2x - \cos^4 2x = -\frac{1}{2}$$

in the interval $0 \leq x \leq 180^\circ$

(7) (a) Show the equation

$$1 + \tan x = 2 \left(\frac{\cos x}{\sin x} \right)$$

can be
written as $\tan^2 x + \tan x - 2 = 0$.

(b) Solve the equation

$$\tan^2 x + \tan x - 2 = 0$$

for $-180^\circ < x \leq 180^\circ$ giving your
answers to 3 significant figures
where appropriate.

(8) Given $\sin \alpha = 0.8$ and

$90^\circ < \alpha < 180^\circ$ find the value of:

(a) $\cos \alpha$

(b) $\tan^3 \alpha$

(c) $\sin \alpha \cos^2 \alpha$

(9) (a) Sketch the graphs

of $y = \sin 2x$ and $y = \cos 2x$ for
 $0 \leq x \leq 2\pi$ on the same set of
axis.

(b) Using your graph show
there are 4 solutions to the
equation $\sin 2x = \cos 2x$ in the
interval $0 \leq x \leq 2\pi$.

(c) Solve the equation

$$\sin 2x = \cos 2x$$

for $0 \leq x \leq 2\pi$
giving your answers as
multiples of π .